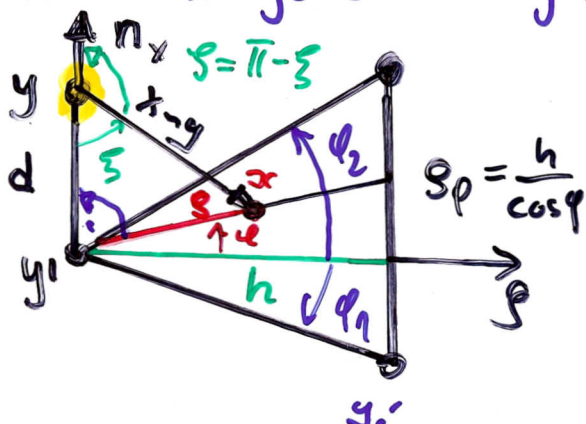


2. y is located on the straight line that is orthogonal to the plane $E(\Gamma_j) \supset \Gamma_j$ and that goes through a vertex of the triangle Γ_j :



$$y = y_i = \vec{y}_i$$

$$\cos \star (x-y, n_x) =$$

$$= \cos \xi =$$

$$= -\cos \xi = -\frac{d}{|x-y|}$$

$$\vec{b}_y = \int_{\Gamma_j} \frac{\partial E}{\partial n_x}(x, y) dS_x = -\frac{1}{4\pi} \int_{\Gamma_j} \frac{(x-y, n_x(x))}{|x-y|^3} dS_x$$

$$= -\frac{1}{4\pi} \int_{\Gamma_j} \frac{\cos \star (x-y, n_x)}{|x-y|^2} dS_x$$

$$\uparrow (x-y, n_x) = \cos \star (x-y, n_x) \cdot |x-y| \cdot \underbrace{|n_x|}_{=1}$$

$$\stackrel{(*)}{=} \frac{d}{4\pi} \int_{\Gamma_j} \frac{dS_x}{|x-y|^3} \stackrel{\uparrow}{=} \frac{d}{4\pi} \int_{\varphi_1}^{\varphi_2} \int_0^{h/\cos\varphi} \frac{s ds d\varphi}{(\sqrt{s^2 + d^2})^3}$$

$$\stackrel{(\uparrow)}{=} -\frac{d}{4\pi} \int_{\varphi_1}^{\varphi_2} \frac{d\varphi}{\sqrt{s^2 + d^2}} \Big|_0^{\frac{h}{\cos\varphi}} = -\frac{d}{4\pi} \left[\int_{\varphi_1}^{\varphi_2} \frac{d\varphi}{\sqrt{\frac{h^2}{\cos^2\varphi} + d^2}} - \int_{\varphi_1}^{\varphi_2} \frac{d\varphi}{|d|} \right]$$

$$= -\frac{d}{4\pi} \left[\int_{\varphi_1}^{\varphi_2} \frac{\cos\varphi d\varphi}{\sqrt{h^2 + d^2 \cos^2\varphi}} - \frac{1}{|d|} (\varphi_2 - \varphi_1) \right] = \dots$$

$$= -\frac{1}{4\pi} \frac{d}{\sqrt{h^2 + d^2}} \int_{\varphi_1}^{\varphi_2} \frac{d(\sin\varphi)}{\sqrt{1 - \frac{d^2}{h^2 + d^2} \sin^2\varphi}} + \frac{1}{4\pi} \operatorname{sgn}(d) (\varphi_2 - \varphi_1)$$

$$x^2 = \frac{d^2}{h^2 + d^2} < 1$$

$$\Downarrow -\frac{1}{4\pi} \int_{\varphi_1}^{\varphi_2} \frac{d(x \sin\varphi)}{\sqrt{1 - (x \sin\varphi)^2}} + \frac{1}{4\pi} \operatorname{sgn}(d) (\varphi_2 - \varphi_1)$$

$$= -\frac{1}{4\pi} \arcsin(x \sin\varphi) \Big|_{\varphi_1}^{\varphi_2} + \frac{1}{4\pi} \operatorname{sgn}(d) (\varphi_2 - \varphi_1).$$