

• Assumptions of Theorem 2.13 ($\Lambda = \Lambda_c$):

1) Standard Assumptions (2.3):

OK
OK

- $F \in X^*$, $G \in \Delta^* = \Lambda$ (more) OK
- $a(\cdot, \cdot)$, $b(\cdot, \cdot)$ + (more) OK
- LBB-condition: \rightarrow nontrivial OK

$$(26) \quad \sup_{v \in H_0^1(\Omega)} \frac{(\operatorname{div} v, p)_0}{\|v\|_1} \geq \beta_1 \|p\|_0 \quad \forall p \in L_2(\Omega)$$

OK

\Rightarrow The LBB-condition (26) is completely equivalent to the LBB-condition for the STOKES problem? OK

OK

- $a(\cdot, \cdot)$ is even X -elliptic, i.e.

$$a(v, v) = 2\mu \|\Sigma(v)\|_0^2 \geq 2\mu C_{K,2}^2 \|v\|_1^2 \quad \forall v \in X$$

↑
Lemma 3.5 (KORN 2) OK

OK

- 2) $a(v, v) \geq 0 \quad \forall v \in X$ and $a(v, v) > 0 \quad \forall v \neq 0$,
 $|a(u, v)| \leq \|u\|_1 \|v\|_1 \quad \forall u, v \in X$, with $\|u\|^2 = a(u, u)$.

OK

- 3) $c(\cdot, \cdot) = (\cdot, \cdot)_0 : \Lambda \times \Lambda \rightarrow \mathbb{R}$:

- $c(p, q) = c(q, p) \quad \forall p, q \in \Lambda$,
- $c(q, q) = \|q\|_0^2 \geq 0 \quad \forall q \in \Lambda$, OK
- $|c(p, q)| \leq \alpha \cdot \|p\|_0 \|q\|_0 \quad \forall p, q \in \Lambda$

• **Theorem 2.3** \Rightarrow

\Downarrow

See T17

$$L(t) := \begin{bmatrix} A & B^T \\ B & -t^2 C \end{bmatrix}$$

1. $L = L(t) : X \times \Lambda \rightarrow X^* \times \Lambda^*$

isomorphism, i.e.

$\exists ! (u, p) \in X \times \Lambda : (24)$

2. $\|L^{-1}(t)\|_{L(X^* \times \Lambda, X \times \Lambda)} \leq c \neq c(t)$