

• Randbedingungen:

$$\Gamma_B: 0 = B \cdot n = \begin{pmatrix} \partial_2 A_3 \\ -\partial_1 A_3 \\ 0 \end{pmatrix} \cdot \begin{pmatrix} n_1 \\ n_2 \\ 0 \end{pmatrix} = \partial_2 A_3 \cdot n_1 - \partial_1 A_3 \cdot n_2$$

$$n = \begin{pmatrix} n_1 \\ n_2 \end{pmatrix}$$



$$\Gamma_B = -\nabla A_3 \times \begin{pmatrix} n_1 \\ n_2 \end{pmatrix} = \frac{\partial}{\partial t} A_3 = 0$$

z.B. $A_3 = 0$ auf Γ_B

$$\Gamma_H: \begin{pmatrix} 0 \\ 0 \\ -J_{i,3} \end{pmatrix} = \underbrace{[\nu(|\nabla \times A|) \nabla \times A]}_{= H} \times n =$$

$$= \nu(|\nabla A_3|) \begin{pmatrix} \partial_2 A_3 \\ -\partial_1 A_3 \\ 0 \end{pmatrix} \times \begin{pmatrix} n_1 \\ n_2 \\ 0 \end{pmatrix}$$

$$= \nu(|\nabla A_3|) \begin{pmatrix} 0 \\ 0 \\ \partial_2 A_3 n_2 + \partial_1 A_3 n_1 \end{pmatrix}$$

• Resultat: 3D Magnetostatik \rightarrow 2D Magnetostatik

Ges. $u = A_3(x) = A_3(x_1, x_2)$:

$$-\text{div}(\nu(x, |\nabla u|) \nabla u(x)) = J_{i,3} + \frac{\mu_0}{\mu} \left(\frac{\partial H_{02}}{\partial x_1} - \frac{\partial H_{01}}{\partial x_2} \right)$$

$x = (x_1, x_2) \in \Omega \subset \mathbb{R}^2$

+ RB auf $\Gamma = \partial \Omega$:

$u = 0$ auf $\Gamma_B = \Gamma_1 = \Gamma_{\text{Dirichlet}}$

$\nu(|\nabla u|) \nabla u \cdot n = -J_{s,3}$ auf $\Gamma_H = \Gamma_2 = \Gamma_{\text{Neumann}}$

• Beispiel: Elektromagnet \rightarrow Folien 12i+j
Elektrische Maschinen