

## Maxwell's equations (differential form)

$$\begin{aligned} \operatorname{curl} \mathbf{E} &= -\frac{\partial \mathbf{B}}{\partial t} && \text{Faraday's law} \\ \operatorname{curl} \mathbf{H} &= \mathbf{J} + \frac{\partial \mathbf{D}}{\partial t} && \text{Ampère's law} \\ \operatorname{div} \mathbf{D} &= \rho && \text{electric Gauss law} \\ \operatorname{div} \mathbf{B} &= 0 && \text{magnetic Gauss law} \end{aligned}$$

## Material laws

$$\begin{aligned} \mathbf{B} &= \mu \mathbf{H} + \mathbf{M} \\ \mathbf{D} &= \varepsilon \mathbf{E} + \mathbf{P} \\ \mathbf{J} &= \sigma (\mathbf{E} + \mathbf{v} \times \mathbf{B}) && \text{Ohm's law} \end{aligned}$$

simplifications in the lecture:

- $\mathbf{M} = \mathbf{P} = \mathbf{v} = 0$
- $\mu, \varepsilon, \sigma$  scalar and only depending on  $\mathbf{x}$  (linear material laws)

## Field quantities and units

<i>quantity</i>	<i>SI unit</i>	<i>description</i>
$\mathbf{B}$	Vs/m <sup>2</sup> = T	magnetic flux density (magnetic induction)
$\mathbf{D}$	As/m <sup>2</sup>	electric flux density (displacement current density)
$\mathbf{E}$	V/m	electric field intensity
$\mathbf{H}$	A/m	magnetic field intensity
$\mathbf{J}$	A/m <sup>2</sup>	electric current density
$\mathbf{J}_{\text{tot}}$	A/m <sup>2</sup>	total current density
$\mathbf{M}$	Vs/m <sup>2</sup> = T	magnetization (remanent flux density)
$\mathbf{P}$	As/m <sup>2</sup>	polarization
$\mathbf{v}$	m/s	velocity
$\varepsilon$	As/Vm	electric permittivity
$\mu$	Vs/Am = H/m	magnetic permeability
$\rho$	As/m <sup>3</sup>	charge density
$\sigma$	A/Vm = 1/Ωm	electric conductivity

units: ampere A, henry H, meter m, tesla T, volt V, ohm Ω, seconds s