

FE-System:

• Symmetric and indefinite formulation:

$$\begin{bmatrix} A_h & B_h^T \\ B_h & -t^2 C_h \end{bmatrix} \begin{bmatrix} \underline{u}_h \\ \underline{p}_h \end{bmatrix} = \begin{bmatrix} \underline{f}_h \\ \underline{0} \end{bmatrix} \quad \text{with } C_h \text{ - mass matrix,}$$

see Subsection 2.4 for iterative solvers!

• Two Schur-Complements are possible:

1. p -Schur-Complement: $\underline{u}_h = -A_h^{-1} B_h \underline{p}_h + A_h^{-1} \underline{f}_h$
 $(B_h A_h^{-1} B_h + t^2 C_h) \underline{p}_h = -A_h^{-1} \underline{f}_h$

2. u -Schur-Complement: $\underline{p}_h = t^{-2} C_h^{-1} B_h \underline{u}_h$
 $(A_h + \lambda B_h^T C_h^{-1} B_h) \underline{u}_h = \underline{f}_h$

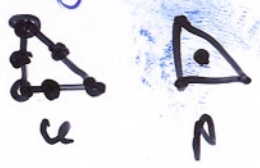
↓ ← maybe, mass lumping!

$$(A_h + \lambda B_h^T \tilde{C}_h^{-1} B_h) \underline{u}_h = \underline{f}_h$$

⇔ ← ∃ element pairs: yes

K_h

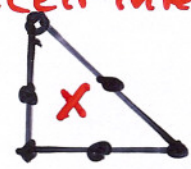
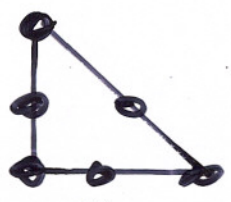
i. e.



$$((A_h + \lambda B_h^T \tilde{C}_h^{-1} B_h) \underline{u}_h, \underline{v}_h) =$$

$$= 2\mu (\varepsilon(\underline{u}_h), \varepsilon(\underline{v}_h))_0 + \lambda (\text{div } \underline{u}_h, \text{div } \underline{v}_h)_{0,h}$$

reduced integration ↗



$$x = \left(\frac{1}{3}, \frac{1}{3}\right)$$

$$\forall \underline{u}_h, \underline{v}_h \in \mathbb{R}^{N_h} : \underline{u}_h, \underline{v}_h \longleftrightarrow \underline{u}_h, \underline{v}_h \in X_h = \bigvee_{DVF} V_{0,h}$$