

b) MVP \Rightarrow SPP

$$\bullet b(u, v) - \langle g, v \rangle = 0 \quad \forall v = \lambda - \mu \in \Delta$$



$$b(u, \lambda) - \langle g, \lambda \rangle \geq b(u, \mu) - \langle g, \mu \rangle \quad \forall \mu \in \Delta$$



$$L(u, \lambda) \geq L(u, \mu) \quad \forall \mu \in \Delta \Leftrightarrow \textcircled{a}$$

$$\bullet u \in X; a(u, v) + b(v, \lambda) = \langle f, v \rangle \quad \forall v \in X, \lambda \in \Delta$$

$$\Updownarrow \leftarrow \text{see a)}$$

$$u \in X: \frac{1}{2} a(u, u) - \langle f, u \rangle + [b(u, \lambda) - \langle g, \lambda \rangle] \leq \\ \leq \frac{1}{2} a(v, v) - \langle f, v \rangle + [b(v, \lambda) - \langle g, \lambda \rangle] \quad \forall v \in X$$



$$L(u, \lambda) \leq L(v, \lambda) \quad \forall v \in X \Leftrightarrow \textcircled{b}$$

q.e.d.