

$$\textcircled{1} \Leftrightarrow b(u, \lambda) - \langle g, \lambda \rangle = 0$$

$$\bullet \textcircled{r} \Leftrightarrow \frac{1}{2} a(u, u) - \langle f, u \rangle + 0 \stackrel{||}{\leq} \frac{1}{2} a(v, v) - \langle f, v \rangle + [b(v, \lambda) - \langle g, \lambda \rangle]$$

$$\Downarrow \quad \forall v \in X$$

1)

$$\frac{1}{2} a(u, u) - \langle f, u \rangle \leq \frac{1}{2} a(u, v) - \langle f, v \rangle \quad \forall v \in \tilde{V}_g$$

$$\textcircled{2} \Leftrightarrow u \in \tilde{V}_g \quad \Updownarrow$$

$u \in \tilde{V}_g : J(u) \leq J(v) \quad \forall v \in \tilde{V}_g$

CMP  
(2P)  
= (30)  
CVP

$$2) \quad \frac{1}{2} a(v, v) - \langle f, v \rangle + [b(v, \lambda) - \langle g, \lambda \rangle] \xrightarrow{v \in X} \min$$

$$\Updownarrow$$

$$\frac{1}{2} a(v, v) - \langle f, v \rangle + b(v, \lambda) \xrightarrow{v \in X} \min$$

$$\Updownarrow$$

Th. I. 2.10 = Th. 1.5 (NUPDE)

$$a(u, v) = \langle f, v \rangle - b(v, \lambda) \quad \forall v \in X$$

$$\Updownarrow$$

$u \in X : a(u, v) + b(v, \lambda) = \langle f, v \rangle \quad \forall v \in X$

• Result: SPP (32)  $\Rightarrow$  MVP (2)

$(u, \lambda) \in X \times M:$   
 $a(u, v) + b(v, \lambda) = \langle f, v \rangle \quad \forall v \in X$   
 $b(u, \mu) = \langle g, \mu \rangle \quad \forall \mu \in \Delta$