

■ Remark 2.1:

1. Instead of Assumption 4) we can also require the more general conditions

$$4a) \sup_{u \in \bar{V}_0 \setminus \{0\}} \frac{a(u, v)}{\|u\|_X} \geq \alpha_1' \|v\|_X \quad \forall v \in \bar{V}_0,$$

$$4b) \sup_{v \in \bar{V}_0 \setminus \{0\}} \frac{a(u, v)}{\|v\|_X} \geq \alpha_1'' \|u\|_X \quad \forall u \in \bar{V}_0.$$

If $a(\cdot, \cdot)$ is symmetric on \bar{V}_0 , then
 $4a) \equiv 4b)$ and $\alpha_1' = \alpha_1''$.

2. In some, practically important problems (e.g. Stokes problem), Assumption 4) can be shown on the whole space X instead of the subspace $\bar{V}_0 \subset X$ only.

3. In Chapter 1, we have already discussed some typical examples leading (naturally or artificially) to mixed variational formulations:

- Example 1.1: the Stokes problem
- Example 1.2: mixed variational formulation of the Dirichlet problem for the Poisson equation
 (\rightarrow Hellinger-Reissner principle)
- Example 1.3: mixed variational formulation of the 1st biharmonic BVP