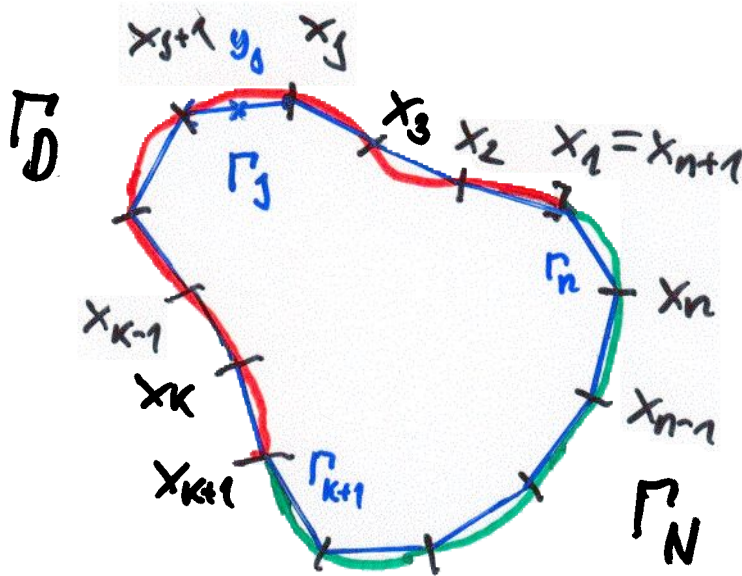


## ■ Discretization of the boundary:

$$\Gamma = \Gamma_D \cup \Gamma_N \approx \Gamma_h = \Gamma_{Dh} \cup \Gamma_{Nh}$$

Let us choose  $n$  different nodes  $x_1, \dots, x_n$  on the boundary  $\Gamma$  of the domain  $\Omega$ :



$$\begin{aligned} x_i &\neq x_j \quad \forall i \neq j \\ x_1, \dots, x_k &\in \Gamma_D \\ x_{k+1}, \dots, x_n &\in \Gamma_N \\ x_{n+1} &= x_1 \quad (\text{periodic}) \end{aligned}$$

$$\Gamma_j = \{x = x_j + t(x_{j+1} - x_j) \in \mathbb{R}^2 : 0 \leq t < 1\} = \Gamma_{hj} \quad \begin{matrix} \nearrow t_{j+1} \\ \searrow t_j \end{matrix}$$

=  $j$ th boundary piece

$$h_j = |\Gamma_j| = |x_{j+1} - x_j| = j\text{th step size,}$$

$$\Gamma_h = \bigcup_{j=1}^n \Gamma_j = \bigcup_{j=1}^n \Gamma_{hj},$$

$$\Gamma_D \approx \Gamma_{Dh} = \bigcup_{j=1}^k \Gamma_j$$

$$\Gamma_N \approx \Gamma_{Nh} = \bigcup_{j=k+1}^n \Gamma_j$$

$$y_j = x_j + \frac{1}{2}(x_{j+1} - x_j)$$