

■ Meshes:

a) Primary mesh: regular triangular mesh
 $\mathcal{T}_\Delta = \{\delta_r : r \in \mathbb{R}_h\}, \quad \bar{\Omega} = \bigcup_{r \in \mathbb{R}_h} \bar{\delta}_r$

b) Secondary mesh: polygonally bounded boxes
 (e.g. MB or PB) corresponding to $\mathcal{T}_\Delta$:
 (see Subsection 3.2):

$$\begin{aligned} \mathcal{T}_\mathcal{H} &= \{\mathcal{H}(x) : x \in \bar{\omega}_h\}, \\ \mathcal{H}(x) &= \text{meas } \mathcal{H}(x) = O(h^2), \\ \bar{\Omega} &= \bigcup_{x \in \bar{\omega}_h} \bar{\mathcal{H}}(x) = \bigcup_{i \in \bar{\omega}_h} \bar{\mathcal{H}}(x^{(i)}) \\ \bigcup_{i \in \bar{\omega}_h} H^1(\mathcal{H}(x)) \cap C(\bar{\mathcal{H}}) & \quad V_0 = \bigcup_{i \in \bar{\omega}_h} H^1(\mathcal{H}(x)) \end{aligned}$$

■ FEM: $\mathcal{T}_\Delta \xrightarrow[\delta_r \xleftarrow[\text{map}]{P_1} \Delta]{P_1} \bar{V}_h = P_1(\mathcal{T}_\Delta) \supset \bar{V}_{0h} = \bar{P}_1(\mathcal{T}_\Delta) = \text{span}\{p^{(i)} : i \in \bar{\omega}_h\}$

(7) FEM

Find $u_L = u_h \in \bar{V}_{0h} : a(u_h, v_h) = \langle F, v_h \rangle \forall v_h \in \bar{V}_{0h}$

$$\longleftarrow u_L = \sum_{i \in \bar{\omega}_h} u^{(i)} p^{(i)}(x)$$

$$\longleftarrow v_h = p^{(k)}, \quad k \in \bar{\omega}_h$$

(7) FEM

Find $\underline{u}_L = \underline{u}_h = [u^{(i)}]_{i \in \bar{\omega}_h} \in \mathbb{R}^{N_h} : K_L \underline{u}_L = \underline{f}_L$

with $K_L = [a(p^{(i)}, p^{(k)})]_{k, i \in \bar{\omega}_h} = K_L^T$ p.d.,
 $\underline{f}_L = [\langle F, p^{(k)} \rangle]_{k \in \bar{\omega}_h} \in \mathbb{R}^{N_h}$.