

### ■ Remark 3.21:

1. We refer to the literature, e.g. Braess (2013), p. 172f, for the proof of the efficiency estimate b)!
  2. Other a posteriori error estimators:
    - 1) Estimators based on the solution of local Dirichlet problems:  
→ Babuška-Rheinboldt (1978)
    - 2) Estimators based on the solution of local Neumann problems:  
→ Bank-Weiser (1985)
    - 3) Estimators based on averaging  $\nabla u_h$ :  
→ Zienkiewicz-Zhou (ZZ) indicator (1987)
    - 4) Hierarchical estimators:  
→ Denflhard-Leinen-Yserentant (1990)
    - 5) Functional type a posteriori error estimators:  
→ Repin (1997) ↓ Friedrichs
$$\|u-v\|_{1,\Omega} \leq \bar{M}(v, \sigma) := \|\sigma - \nabla v\|_{0,\Omega} + c_F(\Omega) \|f + \operatorname{div} \sigma\|_{0,\Omega}$$

$\forall v \in \bar{V}_0$  and  $\forall \sigma \in H(\operatorname{div}, \Omega)$

e.g.  $u_h \in \bar{V}_{0h} \subset \bar{V}_0$       $R_h(\nabla u_h)$  ?
  - 6) Equilibrated error estimators  
→ Braess-Schöberl (2008)
3. Standard literature on a priori error estimators:
    - [1] Verfürth R.: A review of a posteriori error estimation and adaptive mesh refinement techniques. Wiley-Teubner, 1996
    - [2] Repin S.: A priori error estimates for PDEs. RSCAM, de Gruyter, Berlin, 2008.
    - [...] ...