

■ Exercises:

**[Ex 1.1]** = Exercises 01 - 03 of Tutorial 1  
 Formulate the classical assumptions which we have to impose on the data  $\{a_{ij}, b_i, c, \alpha, f, g_i, \Omega\}$  of (5)!  
 Provide sufficient conditions in order to ensure that a generalized solution  $u \in \bar{V}_g \cap X \cap H^2(\Omega)$  of (6) is also a solution of (5) in the classical sense!  
 Consider first the Dirichlet problem for the Poisson equation for the training:

(5)  
Poisson

Find  $u \in X := C^2(\Omega) \cap C(\bar{\Omega})$ :  
 $-\Delta u(x) = f(x), x \in \Omega \subset \mathbb{R}^d$  (f)  
 $u(x) = g(x), x \in \Gamma = \partial\Omega \in C^2$

?  $\Downarrow$   $\Updownarrow$  ?

(6)  
Poisson

Find  $u \in \bar{V}_g := \{v \in V = H^1(\Omega) : v = g \text{ on } \Gamma\}$ :  
 $\underbrace{\int_{\Omega} \nabla^T u \nabla v dx}_{= a(u, v)} = \underbrace{\int_{\Omega} f v dx}_{= \langle F, v \rangle} \forall v \in \bar{V}_0 = H^1_0(\Omega)$

**[Ex 1.2]** = Exercise 04 : Show that in the following cases a) - c) the assumption of the L&M-Th. are satisfied, and compute  $\mu_1$  and  $\mu_2$ ! We assume (7) and

- a)  $b_i = 0; c(x) \geq 0 \quad \forall x \in \Omega; \alpha(x) \geq 0 \quad \forall x \in \Gamma_3; \text{meas}_{d-1}(\Gamma_1) > 0;$
- b)  $b_i = 0; c = 0; \alpha(x) \geq \underline{\alpha} = \text{const} > 0 \quad \forall x \in \Gamma_3, \text{meas}_{d-1}(\Gamma_1) > 0, \Gamma_1 = \emptyset;$
- c)  $b_i \geq 0, c(x) \geq \underline{c} = \text{const} > 0 \quad \forall x \in \Omega, \Gamma = \Gamma_2 \text{ (i.e. } \Gamma_1 = \Gamma_3 = \emptyset\text{)}$