

- Choosing the vector potential A^* in the form

$$A^* = A + \int_0^t \nabla \varphi \, dt,$$

we obtain the following vector potential formulation from (6): $v=0$

$$(6)^* \quad \boxed{\operatorname{curl} v \operatorname{curl} A^* + \sigma \frac{\partial A^*}{\partial t} + \varepsilon \frac{\partial^2 A^*}{\partial t^2} = \tilde{J}_i} \quad \text{in } Q_T = \Omega \times (0, T)$$

with $\tilde{J}_i := J_i - \operatorname{curl} \frac{\mu_0}{\mu} M + \frac{\partial P}{\partial t}$.

Once A^* is determined, the magnetic and electric fields can be calculated as follows:

$$B = \operatorname{curl} A^*, \quad H = v B - \frac{\mu_0}{\mu} M,$$

$$E = -\frac{\partial A^*}{\partial t}, \quad D = \varepsilon E + P.$$

- Boundary Conditions on $\Gamma \times (0, T)$:

1) Perfect Electric Conductors (PEC)

$$A^* \times n = 0 \text{ on } \Gamma_{\text{PEC}} \quad (\Rightarrow E \times n = 0 \text{ on } \Gamma_{\text{PEC}})$$

2) Perfect Magnetic Conductors (PMC)

$$\mu^{-1} \operatorname{curl} A^* \times n = 0 \text{ on } \Gamma_{\text{PMC}} \quad (\Leftrightarrow H \times n = 0 \text{ on } \Gamma_{\text{PMC}})$$

3) Impressed surface currents (ISC)

$$\mu^{-1} \operatorname{curl} A^* \times n = -j_{\text{sc}} \text{ on } \Gamma_{\text{ISC}} \quad (\Leftrightarrow H \times n = -j_{\text{sc}} \text{ on } \Gamma_{\text{ISC}})$$

4) Impedance boundary conditions (IBC)

$$H \times n - \alpha (E \times n) \times n = 0 \text{ on } \Gamma_{\text{IBC}}$$

etc.

- Initial Conditions at $t = t_0 := 0$:

$$A^*(x, 0) = 0 \text{ for } x \in \bar{\Omega},$$

$$\frac{\partial A^*}{\partial t}(x, 0) \equiv -E(x, 0) = E_0(x) \text{ for } x \in \bar{\Omega}.$$