

Theory of optical spectra of photosynthetic pigment-protein complexes: From structure to function

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Introduction: light-harvesting

Theory of spectra and excitation energy transfer

Calculation of parameters

Applications: B777-complex, B820-complex, WSCP, FMO-Protein, Photosystem I

Harvesting sun light

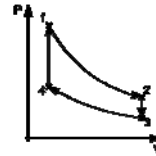
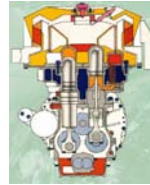


<http://www.en.tibet.cn>

Solar thermal power

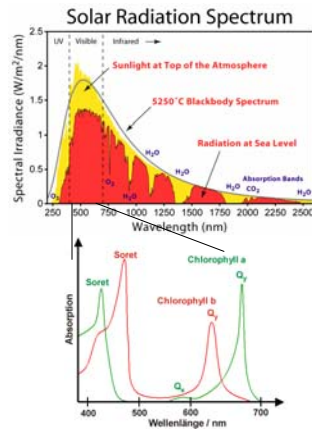
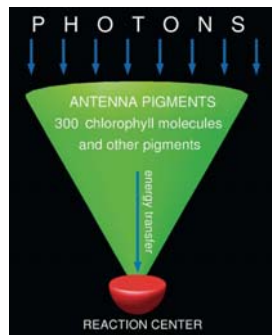
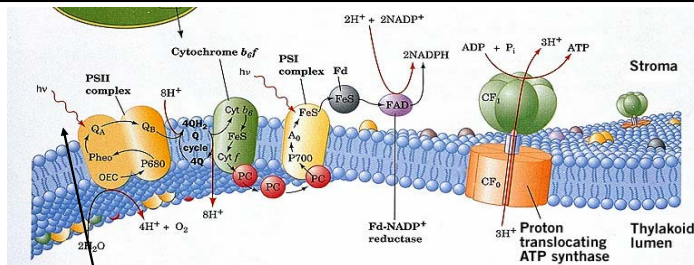
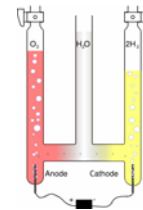


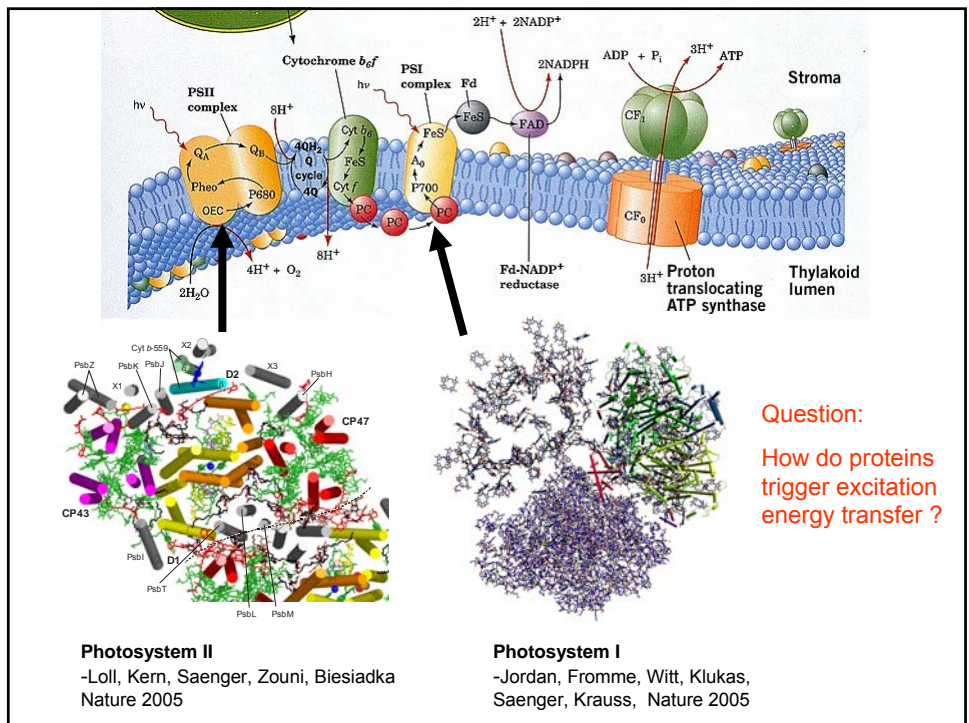
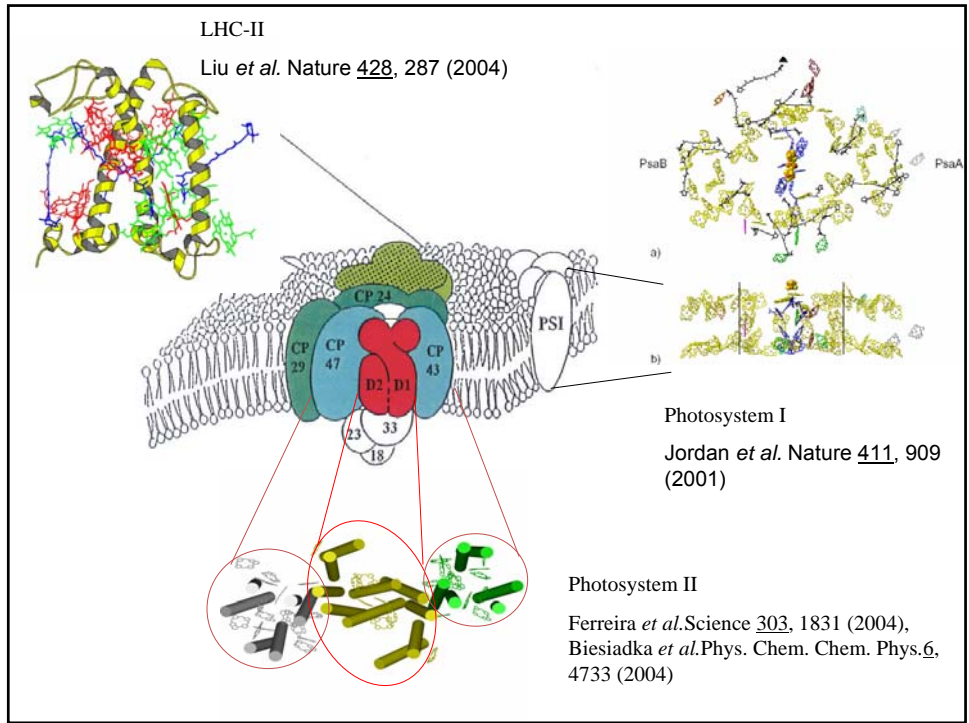
Sterling engine



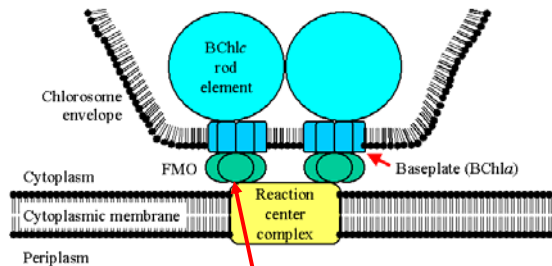
Using thermal power to generate electricity

Using electricity to split water and store energy as hydrogen fuel (1 kg H₂ per day)

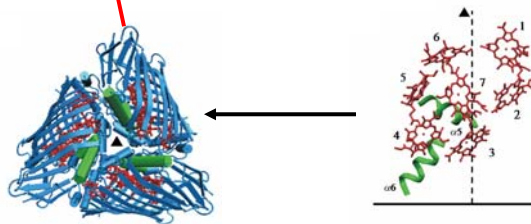




Light harvesting in green sulfur bacteria: The role of pigment-protein coupling

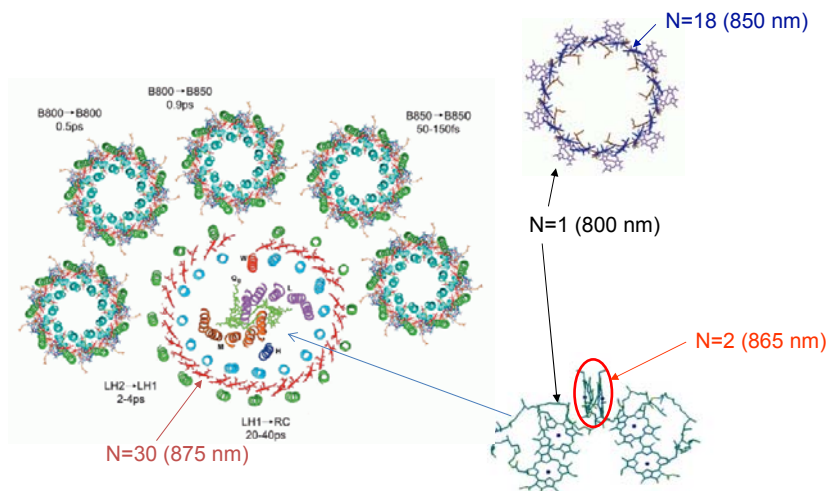


- Fenna *et al.* *Nature* 1975,
- Tronrud *et al.* *J. Mol. Biol.* 1986 (1.9 Å)



Question: How is excitation energy flow directed in the FMO protein ?

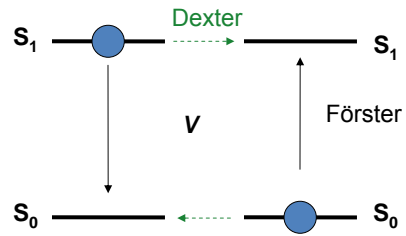
Light-harvesting in purple bacteria: The role of pigment-pigment coupling



Question: Why is excitation energy of special pair (N=2) so low?

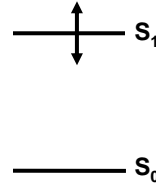
Interactions in Pigment-Protein Complexes

Pigment-Pigment Coupling



- Excitation energy transfer
- Delocalized excited states
- Coupling to charge transfer states

Pigment-Protein Coupling



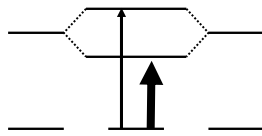
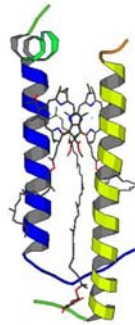
- Different site energies
- Dynamic modulation of site energies
- Static disorder

Model systems

B777 complex

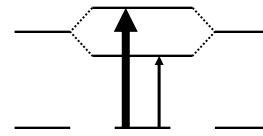
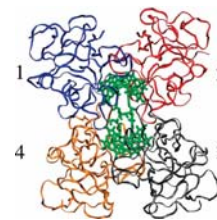


B820 complex

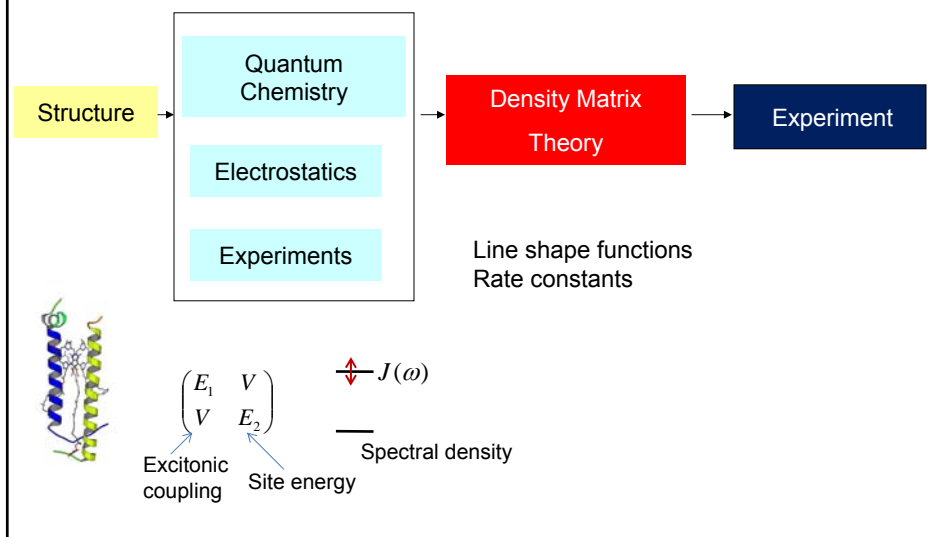


IIB-WSCP

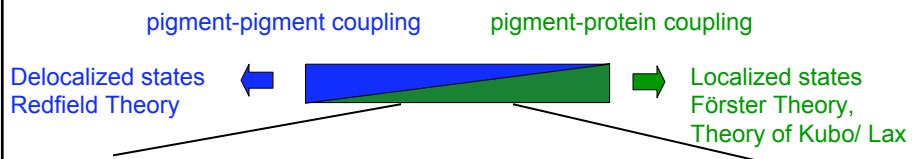
Horigome *et al.*
J. Biol. Chem. 2007



Development of theory and calculation of parameters



Theories of optical spectra and excitation energy transfer



- **Generalized Förster Theory** (Fetisova et al. 1996, Sumi et al. 1999, Jang et al. 2004, Raszewski, Renger *et al.* 2005, Raszewski and Renger 2008), **Transfer between aggregates**
- **Modified Redfield Theory** (Mukamel and coworkers 1998, Yang und Fleming 2002, Renger und Marcus 2003, ...), **Excitonic potential energy surfaces**
- **Non-Markovian Density Matrix Theory** (Zwanzig 1960, van Kampen 1974, Renger and May 2001, Renger and Marcus 2002, Jang and Silbey 2003, Renger 2004), **Vibrational sidebands and life time broadening, dynamic localization**

Non-Markovian Expressions for Linear Absorption

COP-Theory (Renger and May, Phys. Rev. Lett. 84, 5228 (2000))

$$D_M(\omega) = \frac{\Gamma_M(\omega)}{(\omega - \tilde{\omega}_M)^2 + (\Gamma_M(\omega))^2}$$

$$\Gamma_M(\omega) = \sum_K \gamma_{MK} \pi(\omega - \omega_{K0})^2 \{ (1 + n(\omega - \omega_{K0})) J(\omega - \omega_{K0}) + n(\omega_{K0} - \omega) J(\omega_{K0} - \omega) \}$$

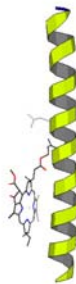
POP-Theory (Renger and Marcus, J. Chem. Phys. 116, 9997 (2002))

$$D_M(\omega) = \Re \int_0^\infty dt e^{i(\omega - \tilde{\omega}_M)t} e^{G_M(t) - G_M(0)} e^{-t/\tau_M}, \quad \tau_M^{-1} = \Gamma_M(\omega_{M0})$$

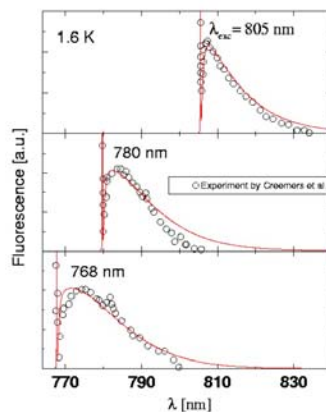
$$G_M(t) = \gamma_{MM} \int_0^\infty d\omega J(\omega) \{ (1 + n(\omega)) e^{-i\omega t} + n(\omega) e^{i\omega t} \}$$

Extraction of Spectral Density of Monomer Complex

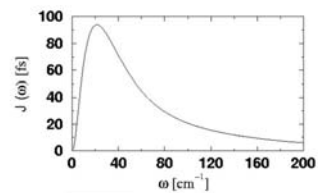
B777 Complex



FLN Spectra



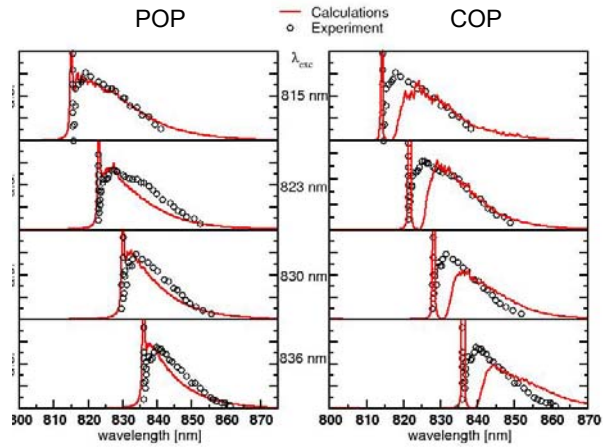
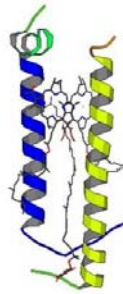
Spectral Density



Renger and Marcus, J. Chem. Phys. 116, 9997 (2002)

Calculation of Fluorescence Line Narrowing Spectra of Dimer Complex

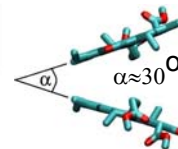
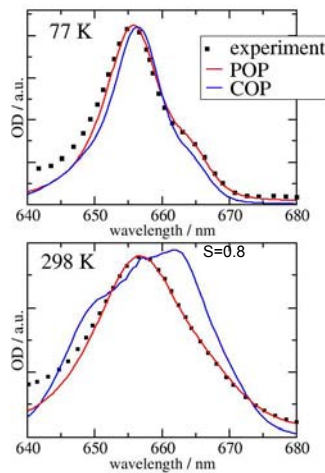
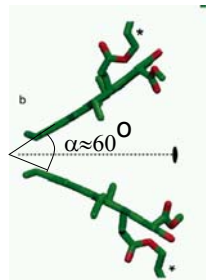
B820 Complex



Renger and Marcus, J. Chem. Phys. 116, 9997 (2002)

Structure Prediction of WSCP

Structural model for IIA-WSCP-complex with Chl *a* / Chl *a* of cauliflower

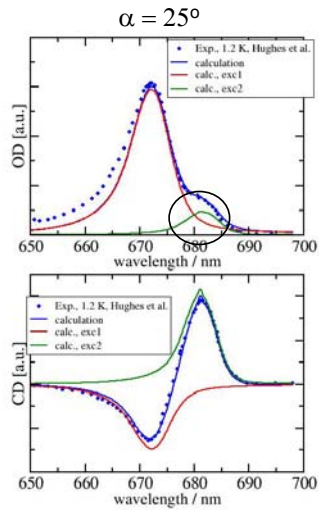


Structural model for IIA-WSCP-complex with Chl *b* / Chl *b* of cauliflower

Hughes et al., JACS (2006)

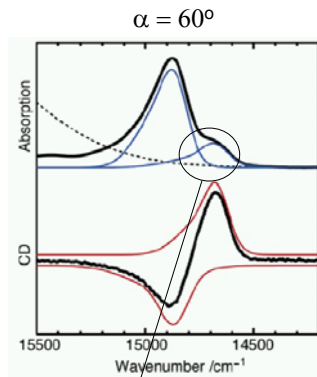
Renger, Trostmann *et al.* JPCB (2007)

Chla-Chla WSCP Revisited



Renger, Trostmann *et al.* JPCB (2007)

Hughes *et al.*, JACS (2006)



Neglect of homogenous broadening !

Comparison theoretical prediction of IIA-WSCP - crystal structure of IIB-WSCP

$\alpha = 27^\circ$



$\alpha = 25^\circ$

Crystal structure of
Chla/Chla dimer in
IIB WSCP-complex



Structural model for
Chla/Chla dimer in
IIA-WSCP-complex
of cauliflower

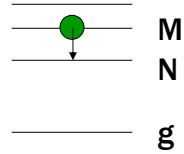
Horigome *et al.*
J. Biol. Chem. (2007)



Renger, Trostmann *et al.*
JPCB (2007)

-> IIA-WSCP and IIB-WSCP share the same Chl binding motif

Rate Constant for Transitions between Delocalized States- Redfield Theory



Exciton relaxation

$$k_{M \rightarrow N} = 2\pi\gamma_{MN}\omega_{MN}^2 \{J(\omega_{MN})[1+n(\omega_{MN})] + J(\omega_{NM})n(\omega_{NM})\}$$

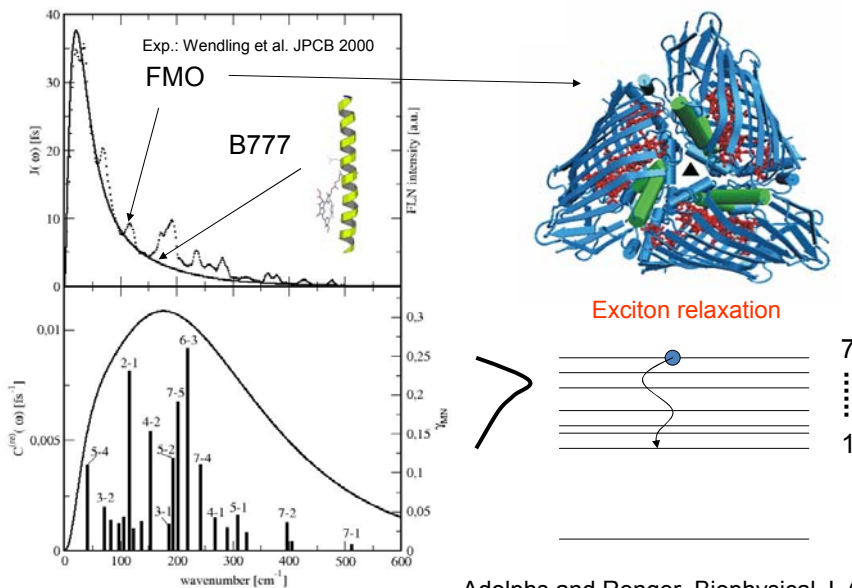
$$\gamma_{MN} = \sum_m |c_m^{(M)}|^2 |c_m^{(N)}|^2$$

Lineshape function for optical excitation (Markov approximation)

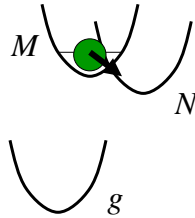
$$D_M(\omega) = \frac{\tau_M^{-1}}{(\omega - \tilde{\omega}_M)^2 + \tau_M^{-2}} \quad \tau_M^{-1} = \frac{1}{2} \sum_N k_{M \rightarrow N}$$

e.g. Renger, May and Kühn, *Physics Rep.* **343**, 137 (2001)

Spectral density and exciton relaxation



Modified Redfield Theory



-Non-perturbative treatment of diagonal part of exciton vibrational coupling (excitonic PES)

-Brownian oscillators: Mukamel and coworkers (1998), Yang and Fleming (2002)

-Harmonic oscillators: Renger and Marcus (2003)

Rate Constant in Modified Redfield Theory

$$k_{M \rightarrow N} = \int_{-\infty}^{\infty} dt e^{i\omega_{MN}t} e^{\phi_{MN}(t) - \phi_{MN}(0)} \left[\left(\frac{\lambda_{MN}}{\hbar} + G_{MN}(t) \right)^2 + F_{MN}(t) \right]$$

with

$$\phi_{MN}(t) = \phi_0(t) \sum_m (|c_m^{(M)}|^2 - |c_m^{(N)}|^2)^2$$

$$G_{MN}(t) = -i\dot{\phi}_0(t) \sum_m ((c_m^{(M)})^3 c_m^{(N)} - (c_m^{(N)})^3 c_m^{(M)})$$

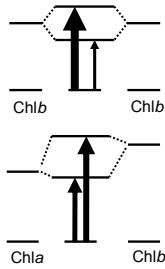
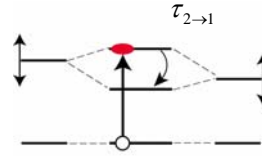
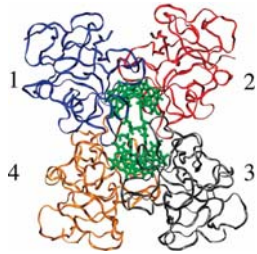
$$F_{MN}(t) = -\ddot{\phi}_0(t) \sum_m |c_m^{(M)}|^2 |c_m^{(N)}|^2$$

$$\lambda_{MN} = \frac{\lambda}{2} \sum_m ((c_m^{(M)})^3 c_m^{(N)} + (c_m^{(N)})^3 c_m^{(M)})$$

$$\phi_0(t) = \int_{-\infty}^{\infty} d\omega J(\omega) \{ (1+n(\omega)) e^{-i\omega t} + n(\omega) e^{i\omega t} \}$$

Renger and Marcus J. Phys. Chem. A 107, 8404 (2003)

Exciton relaxation in WSCP

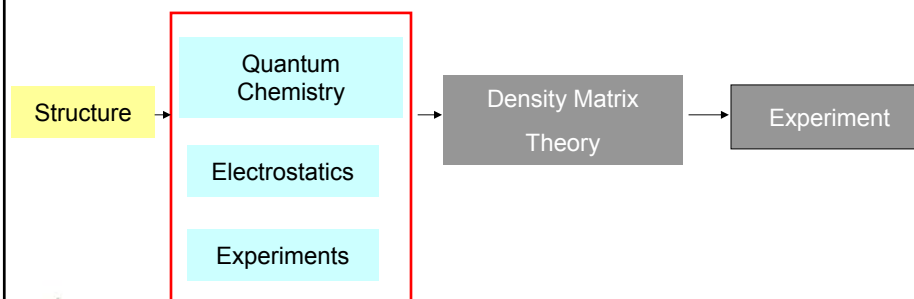


	Mod. Redfield (Renger <i>et al.</i> 2007)	Redfield (Renger <i>et al.</i> 2007)	Experiment (Theiss <i>et al.</i> 2007)
Chlb/ Chlb	60 fs	80 fs	< 150 fs
Chla/ Chlb	450 fs	5400 fs	400 fs

Multi vibrational
quanta-transitions
included

Only one
quantum-
Transitions
included

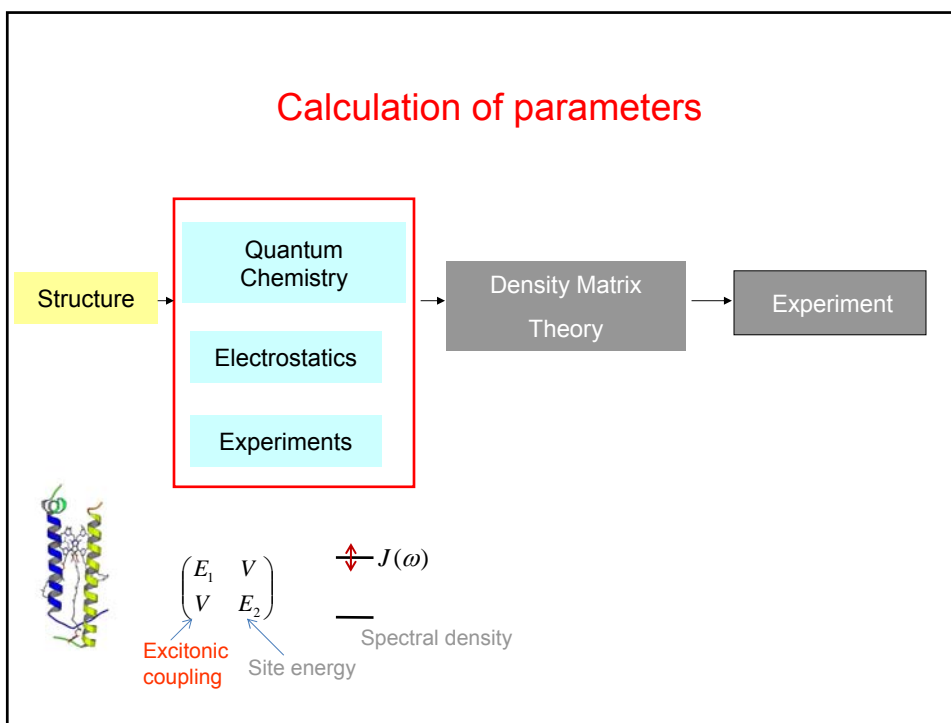
Calculation of parameters



$$\begin{pmatrix} E_1 & V \\ V & E_2 \end{pmatrix} \quad \longleftrightarrow \quad J(\omega)$$

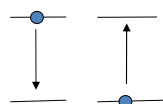
Excitonic coupling
Site energy
Spectral density

Calculation of parameters

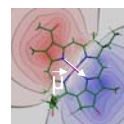


Excitonic coupling

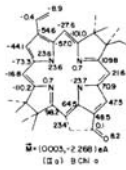
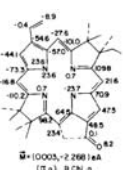
Point dipole approximation



$$V_{mn} = f \left(\frac{\vec{\mu}_m \vec{\mu}_n}{R_{mn}^3} - 3 \frac{(\vec{\mu}_m \vec{R}_{mn})(\vec{\mu}_n \vec{R}_{mn})}{R_{mn}^5} \right)$$

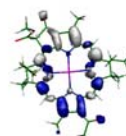
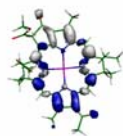


Transition monopole method (Weiss 1972, Chang 1977)



$$V_{mn} = f \sum_{I,J} \frac{q_I^{(m)} q_J^{(n)}}{|\vec{R}_I - \vec{R}_J|}$$

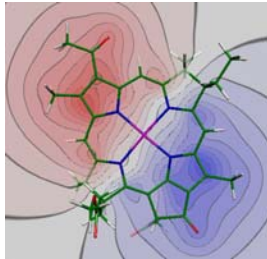
Transition density cube (TDC) method (Krüger, Scholes, Fleming 1998)



$$V_{mn} = f \int d^3 r_1 d^3 r_2 \rho_m(\vec{r}_1) \frac{1}{|\vec{r}_1 - \vec{r}_2|} \rho_n(\vec{r}_2)$$

Transition charges from electrostatic potential (TrEsp) method

ESP of transition density
BChl a (TDDFT/B3LYP)

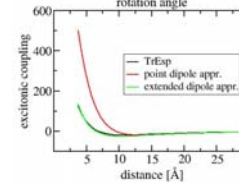
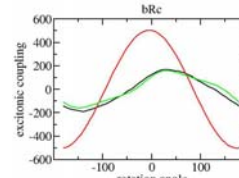
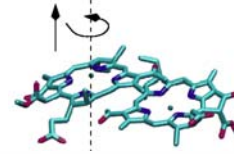


Fit of ab-initio ESP of transition density by atomic partial charges

$$V_{mn} = f \sum_{I,J} \frac{q_I^{(m)} q_J^{(n)}}{|\vec{R}_I - \vec{R}_J|}$$

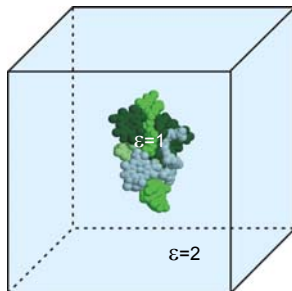
Madjet, Abdurahman, Renger, JPC B (2006)

Special pair coupling in bRc



Dipole extent: 8.8 Å

Influence of the dielectric medium on excitonic couplings



Continuum electrostatics calculations on FMO protein

- BChls treated as cavities with transition monopole charges in dielectric of protein/ solvent, $\epsilon = 2$

- $|\mu_{\text{vac}}|^2 = 37 D^2$ (Knox and Spring 2003)

$$\nabla[\epsilon(\vec{r})\nabla\phi_m(\vec{r})] = -4\pi \sum_I q_I \delta(\vec{r} - \vec{R}_I^{(m)})$$

$$V_{mn} = \sum_I q_I \phi_m(\vec{R}_I^{(n)})$$

effective dipole strength

$$V_{mn}(\epsilon = 2) = f V_{mn}^{(\text{vac})}$$

f : screening / local field correction

Result for FMO: $f = 0.8 \rightarrow |\mu_{\text{eff}}|^2 = 30 D^2$

Renger and Adolphs, Biophys. J. 2006

Direct calculation of site energies

Quantum chemical calculations

Eccles and Honig 1983 (model study)

Gudowska-Nowak, Newton, Fajer 1990
(FMO, N=7)

Damjanovic, Vaswani, Fromme,
Fleming 2002 (PS-I, N=96)

No long-range electrostatic interactions
with the protein included

$$\begin{pmatrix} E_1 & & & & \\ & E_2 & & & \\ & & \ddots & & \\ & & & & V_{mn} \\ V_{mn} & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & E_N \end{pmatrix}$$

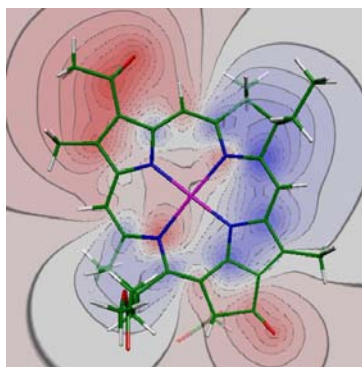
Yin, Dahlbom, Canfield, Hush, Kobayashi, Reimers 2007 (PS-I, N=96)

Protein included by classical point
charges-electron leakage problems

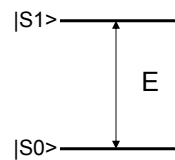
Quantum chemical/ electrostatic approach

Müh, Renger *et al.* 2007, Adolphs, Renger *et al.* 2008

Tuning of site energies by the protein

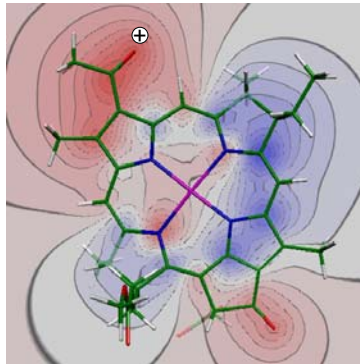


$\phi(S1)-\phi(S0)$, BChl a

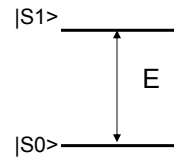


Madjet, Abdurahman, Renger, JPC B 2006

Tuning of site energies by the protein

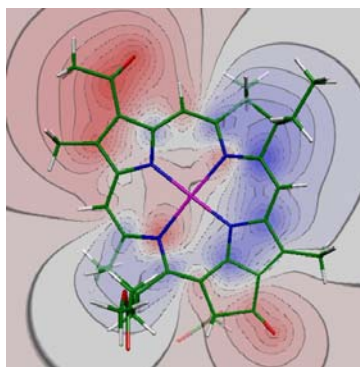


$\phi(S1) - \phi(S0)$, BChl *a*

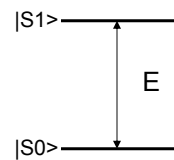


Madjet, Abdurahman, Renger, JPC B 2006

Tuning of site energies by the protein

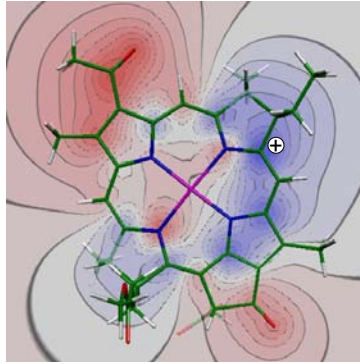


$\phi(S1) - \phi(S0)$, BChl *a*

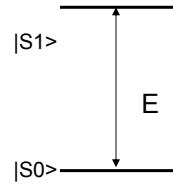


Madjet, Abdurahman, Renger, JPC B 2006

Tuning of site energies by the protein



$\phi(S1)-\phi(S0)$, BChl a

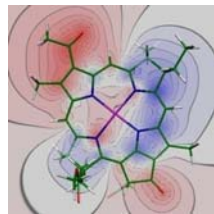


Madjet, Abdurahman, Renger, JPC B 2006

Excitation energy transfer in the FMO-protein

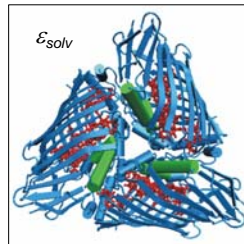
The role of the pigment-protein coupling

Quantum Chemistry



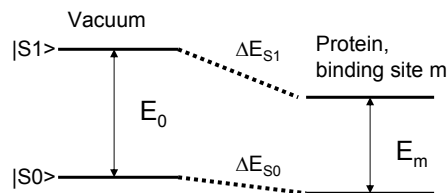
$\phi(S1)-\phi(S0)$, BChl a
(TDDFT/B3LYP)

Atomic Electrostatics

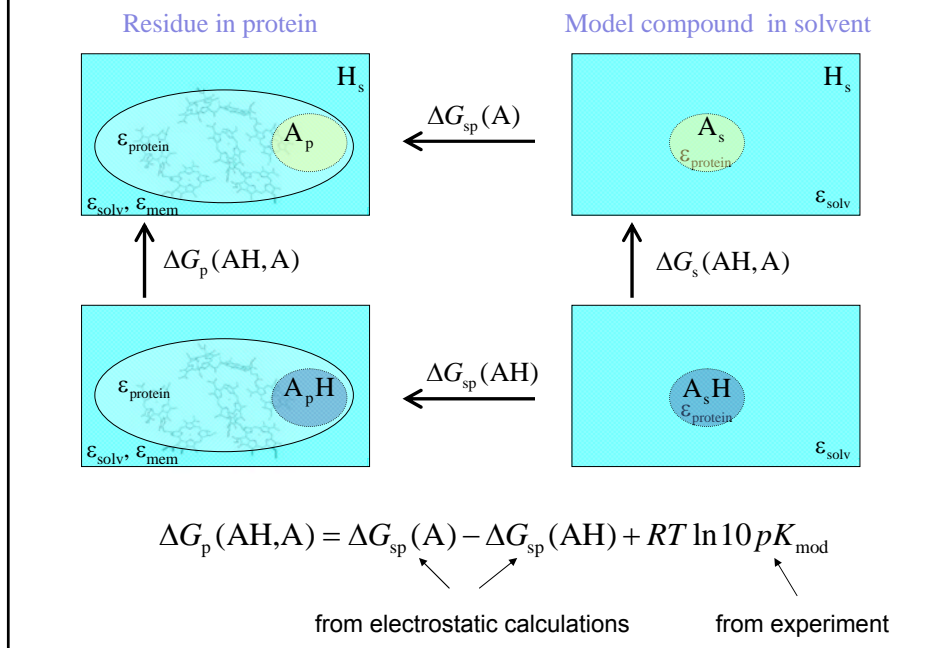


FMO-Protein

- Electrostatic free energy calculations
- Average over protonation states of titratable groups



Thermodynamic cycle for protonation



Continuum electrostatics calculations

$$\nabla[\epsilon(\mathbf{r})\nabla\phi(\mathbf{r})] = -4\pi\rho(\mathbf{r}) + \kappa^2(\mathbf{r})\phi(\mathbf{r})$$

- solving the linearized Poisson-Boltzmann equation numerically
- calculation of ΔG_{sp}(A), ΔG_{sp}(AH) and interaction matrix W_{ij} between titratable groups :

$$\Delta G_p(AH, A) = \Delta G_{sp}(A) - \Delta G_{sp}(AH) + RT \ln 10 pK_{mod}$$

$$\Delta G_p(AH, A), W_{ij}$$

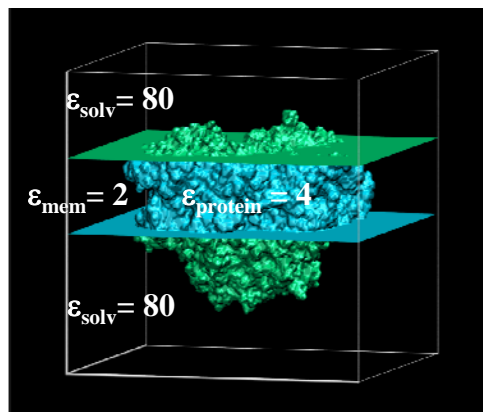


Protonation probability

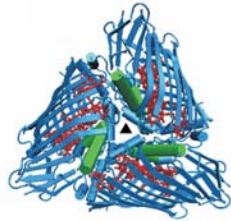
$$\langle x_i \rangle_{proton} = \sum_{x_1 \dots x_N = 0,1} e^{-\frac{\Delta G(x_1 \dots x_N)}{kT}} x_i$$

$$\Delta G(x_1 \dots x_N) = f(pH, \Delta G_p^{(i)}(AH, A), \{W_{ij}\})$$

average performed numerically by Monte Carlo method

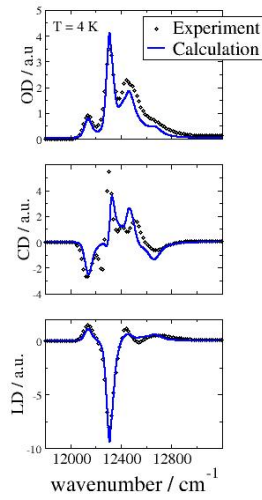


Results for the FMO-Protein



Dominating contributions to site energy shifts

- hydrogen bonds ($<150 \text{ cm}^{-1}$)
- charged amino acid side chains ($<180 \text{ cm}^{-1}$)
- backbone of two α -helices (-340 cm^{-1} at Bchl a 3)



Experiment:
Wendling *et al.*
Photos. Res. 2002

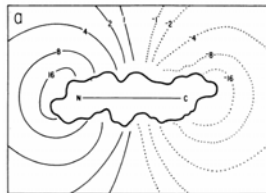
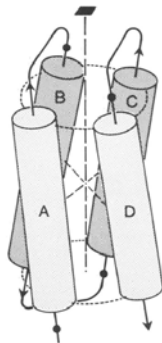
Müh, Renger *et al.* PNAS 2007

Proc. Natl. Acad. Sci. USA
Vol. 79, pp. 4545-4549, August 1982
Biochemistry

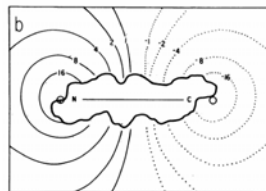
α -Helix dipole model and electrostatic stabilization of 4- α -helical proteins

(electrostatic interactions/protein structure)

ROBERT P. SHERIDAN*, RONALD M. LEVY*†, AND F. R. SALEMME*‡§

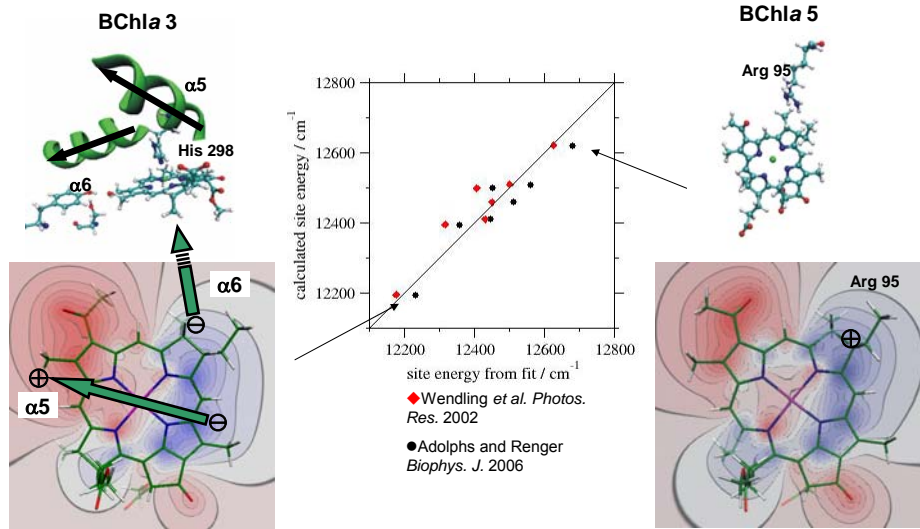


ESP of α -helix

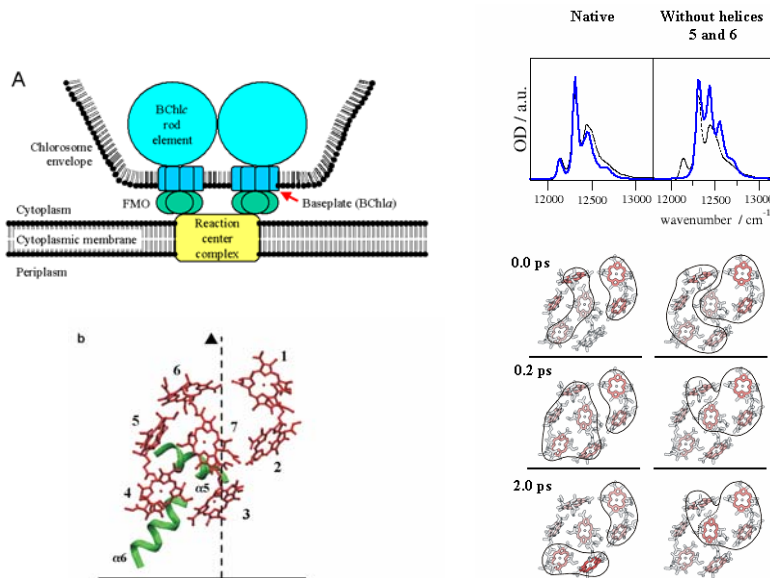


ESP of extended dipole, $|\delta q|=0.5 e$

Correlation between fitted site energies and direct calculations

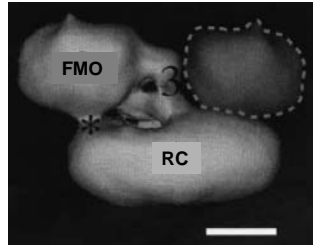


Exciton relaxation between baseplate and reaction center

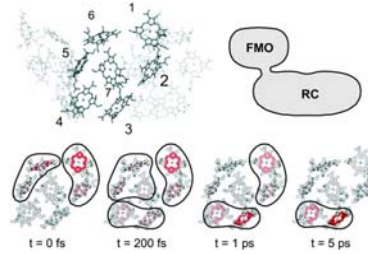


Müh, Renger *et al.* PNAS 2007

Prediction of orientation of FMO-complex



Remigy et al. J. Mol. Biol. 1999

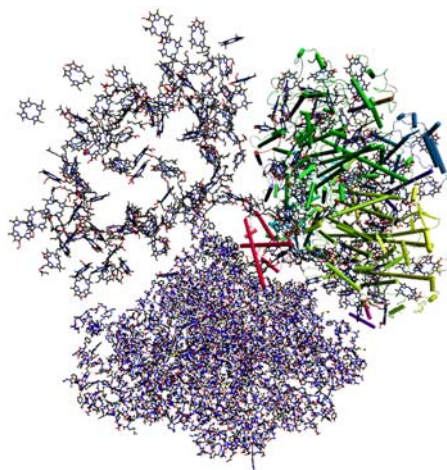


Adolphs and Renger Biophys. J. 2006

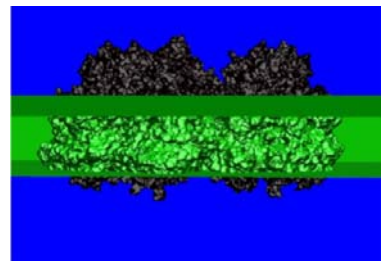
Adolphs and Renger (*Biophys. J.* 2006): „ Efficient transfer of excitation energy to the reaction center requires BChl 3 and 4 to be the linker pigments.”

Wen, Blankenship et al. (*PNAS* 2009): Membrane orientation of the FMO antenna protein from *Chlorobaculum tepidum* as determined by mass spectrometry-based footprinting: „ The large differences in the modification of certain peptides show that the Bchl a #3 side of the FMO trimer interacts with the cytoplasmic membrane, which is consistent with recent theoretical predictions. “

Application to Photosystem I

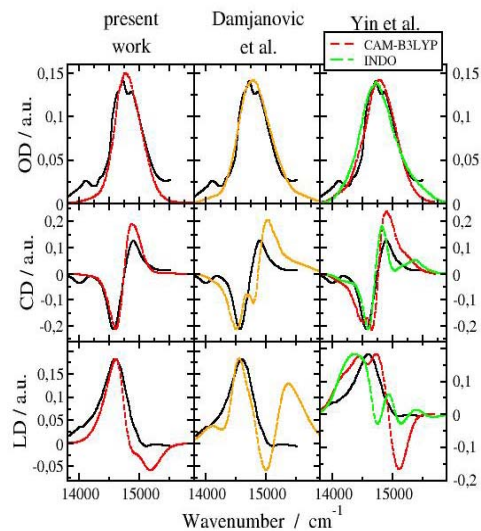


$$N_{\text{Chl}} = 96 * 3$$



Regions of different dielectric constants

Comparison of present approach with quantum chemical calculations from the literature



Damjanovic et al. *J. Phys. Chem. B* 2002

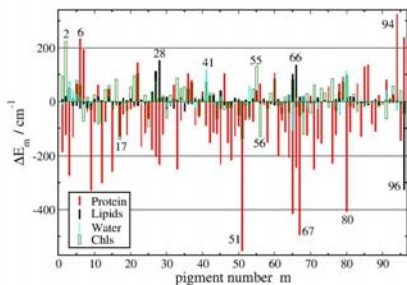
Yin et al. *J. Phys. Chem. B* 2007

Present work: Adolphs, Müh, Madjet, Schmidt am Busch, Renger submitted

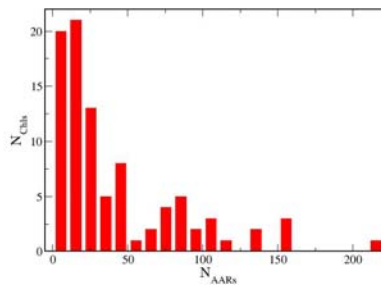
Experiment (black): Byrdin et al. *Biophys. J.* 2002

Cause of site energy shifts

Protein-induced shifts dominate

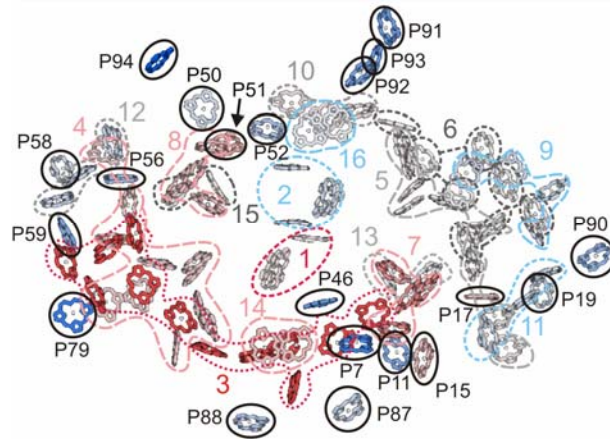


Long-range electrostatic interactions are important



Number of Chls N_{Chl} for which N_{AAR} residues contribute significantly to site energy shift

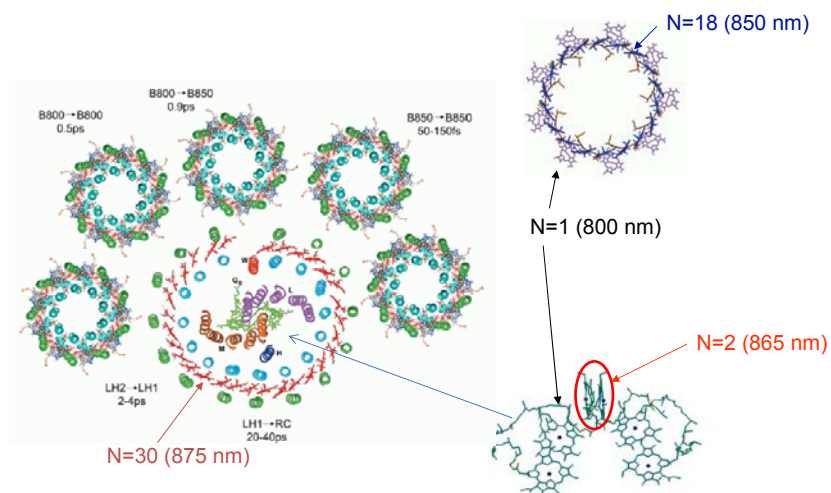
Location of low-energy exciton states



Concentration of low-energy states is higher at the side of the A-branch of the reaction center

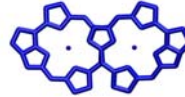
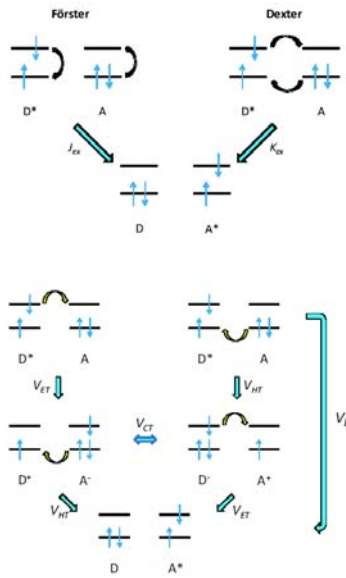
Asymmetric light-harvesting

Analysis of short-range effects



Question: Why is excitation energy of special pair (N=2) so low?

Analysis of short-range interactions between chlorophylls



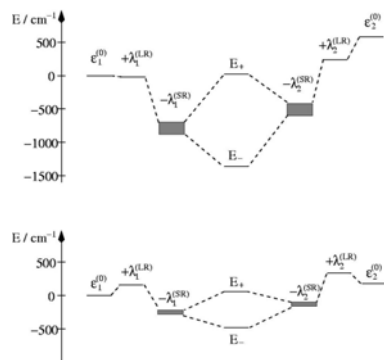
Special pair of purple bacteria

$$H_2 = \begin{pmatrix} \mathcal{E}_1^{(0)} + \lambda_1^{(LR)} + \lambda_1^{(SR)} & V_{LR} + V_{SR} \\ V_{LR} + V_{SR} & \mathcal{E}_2^{(0)} + \lambda_2^{(LR)} + \lambda_2^{(SR)} \end{pmatrix}$$

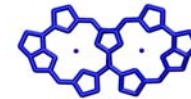
Effective 2-state Hamiltonian relating monomer and dimer quantum chemical calculations

Madjet, Müh, Renger *J. Phys. Chem. B* 2009

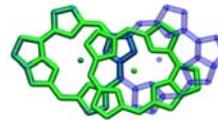
Analysis of short-range effects in special pairs of purple bacteria and photosystem I



bRC

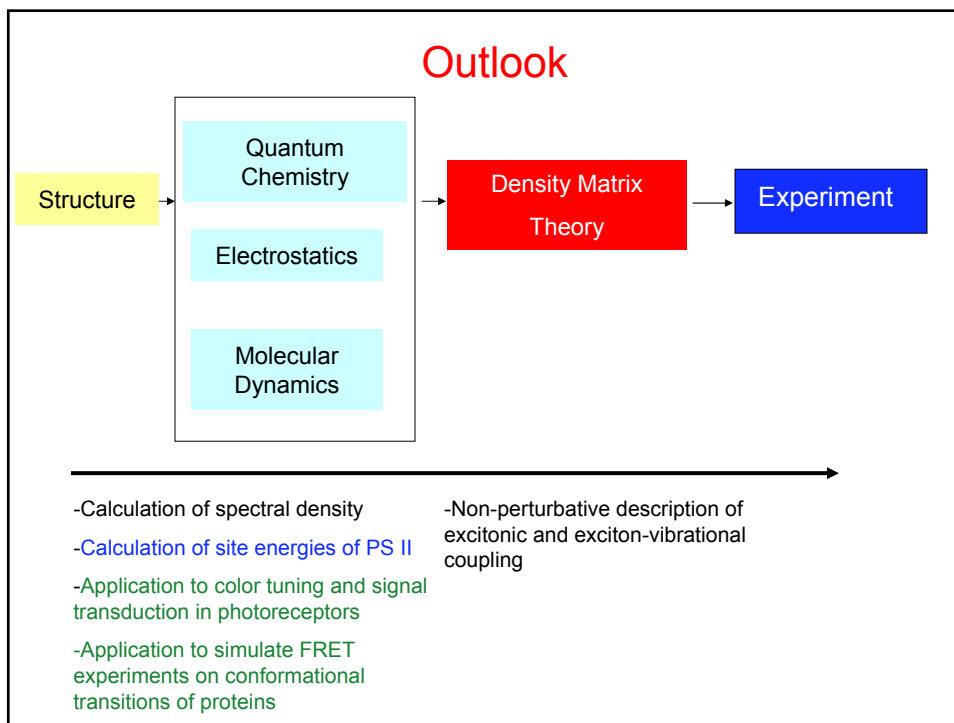
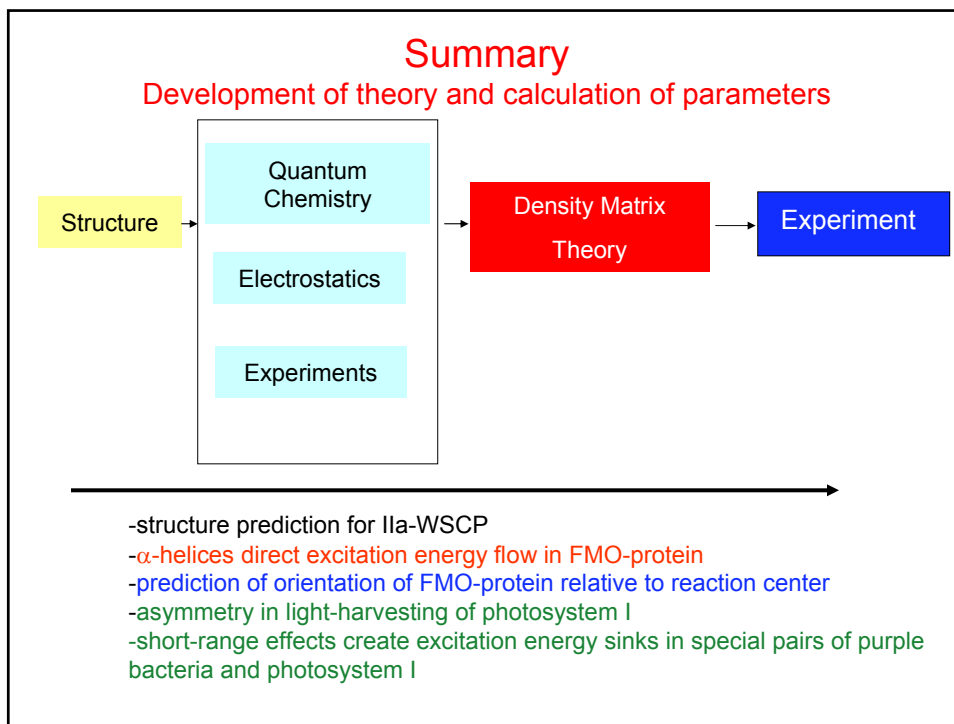


PSI



Short-range effects create excitation energy sink in the special pairs

Madjet, Müh, Renger *J. Phys. Chem. B* 2009



Acknowledgement

Theory of optical spectra:

V. May (Humboldt Universität zu Berlin)
R. Marcus (Caltech, Pasadena)

Quantum chemical
calculations:

M. E. Madjet, Qchem-Developers (Y. Shao, S. T. Brown)

Electrostatic calculations:

E. W. Knapp, G. Kieseritzky (FU Berlin)
F. Müh, J. Adolphs (FU Berlin)
M. Schmidt am Busch (JKU)

Calculation of spectra:

J. Adolphs, G. Raszewski

Experiments, WSCP:

I. Trostmann (Mainz), C. Theiss (TU Berlin)

Experiments, PS-I:

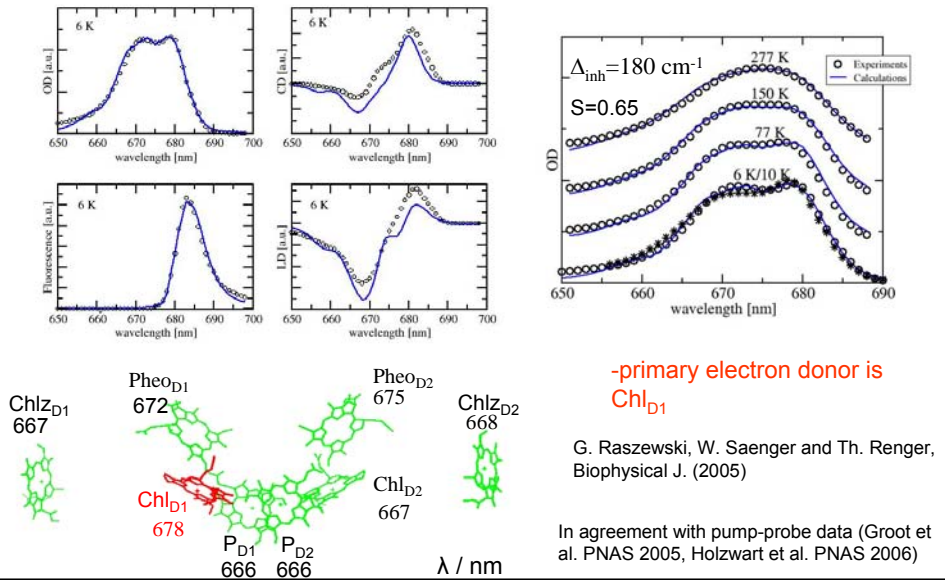
E. Schlodder (TU-Berlin)

Financial support: Deutsche Forschungsgemeinschaft

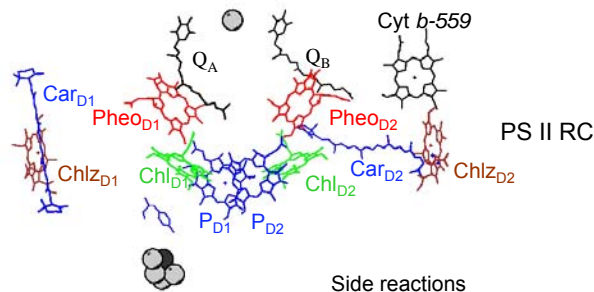


Optical properties of photosystem II reaction centers

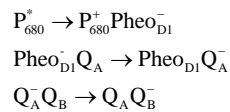
Experiments: Germano et al. (2001)



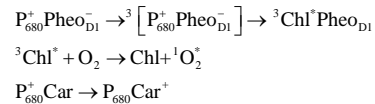
Electron transfer in photosystem II



Primary reactions



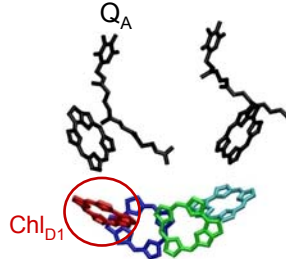
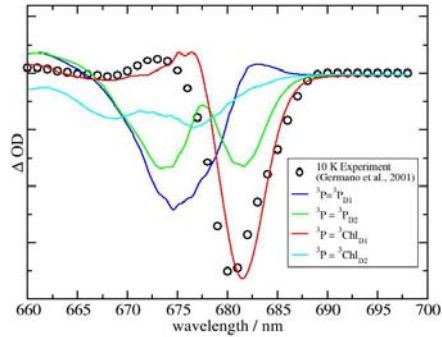
Side reactions



Questions: Nature of P_{680}^* , P_{680}^+ , ${}^3Chl^*$, Car^+
Photoprotective mechanisms,

Localization of the triplet state

Triplet minus singlet absorbance difference



-Triplet localized at Chl_{D1}

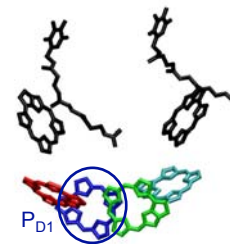
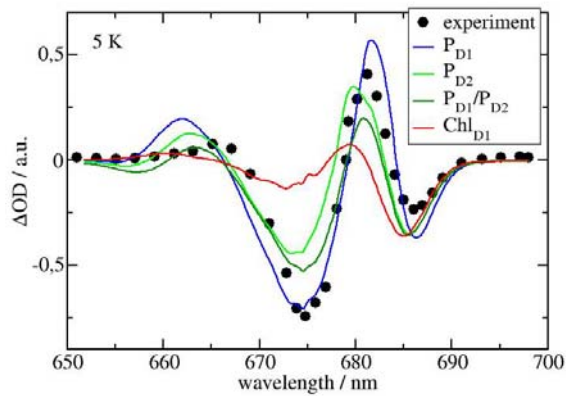
-in agreement with EPR measurements by Rutherford et al. 1991, T-S spectra on mutants by Schlodder, Renger et al. 2008

Photoprotection: ${}^3\text{Chl}_{D1}^* \text{Q}_A^- \rightarrow \text{Chl}_{D1} \text{Q}_A^-$

Theory: G. Raszewski, W. Saenger and Th. Renger, Biophysical J. (2005)

Identity of P₆₈₀⁺

P⁺Q_A⁻ - PQ_A absorbance difference of PS-II Core-Complexes of *T. elongatus*



Hole stabilizes at P_{D1}

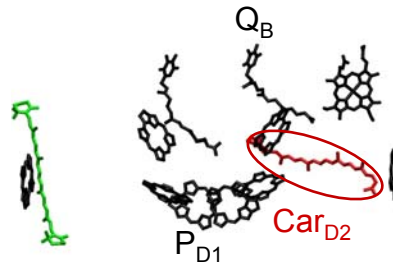
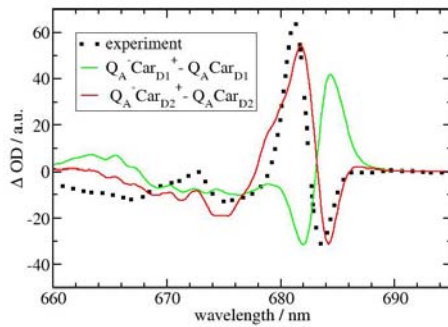
-in agreement with EPR measurements by Zech et al. 1997

-P⁺Q_A⁻-PQ_A spectra on mutants by Diner and Schlodder et al. (2001)

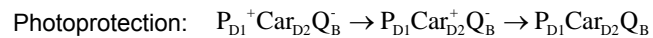
Experiment: Hillmann and Schlodder Biochemistry (1995)

Theory: Raszewski, Diner, Schlodder, Renger Biophys. J. (2008)

Identity of Car⁺

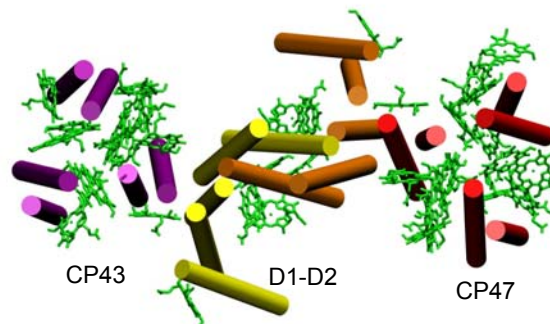


Hole transfer along Car_{D2}



Experiment and theory: Schlodder, Renger et al. Biochemistry (2008)

Light-harvesting in PS-II core complexes



- Site energies obtained from fit of optical spectra of the subunits
- Site energies of CP43 and CP47 verified by calculation of pump-probe spectra and comparison with experimental data
- Question: What limits the decay of excited states ?

Raszewski and Renger JACS (2008)

